

$$b^0 = 1 \text{ except } 0^0$$

$$\sqrt{n} \rightarrow \sqrt{x} \approx \frac{1}{2}(a+\frac{x}{a})$$

Section 1.4 - Defining a Power • 25

8. Evaluate HW P.25 Q8-12 (Right)

a) 5^3 Quiz on Monday (12-1.4) 3^3 c) 6^2 d) 2^6 To solve $4 + 2 \times 3$, do we? _____ If we add first, the answer is 18. If we multiply first, the answer is 10. What if we write $2(3+4)$? Does it make sense? What does the brackets mean? What about $6^2 = 21$? Come to a answer that everyone can agree on. _____e) $(-3)^4$ To standardize the code in _____ f) -3^4 Mathematical operations. _____g) -2^3 Order of Operations _____ h) $-(2^3)$ _____i) -2^6 It occurs, do the exponent _____ j) $-(2^6)$ _____k) $2^0 + 3^0$ _____ l) $2^0 - 3^0$ _____9. Evaluate. $a \neq 0$, $b \neq 0$, $a \neq b$, $a+b \neq 0$

P25

a) 6^0 Order of operations. _____ b) $(-6)^0$ _____c) $-(6)^0$ _____ d) -6^0 _____e) $2^0 + 3^0$ _____ f) $2^0 - 3^0$ _____g) $-2^0 - 3^0$ _____ h) $(2^0 + 3^0)^0$ _____i) $-(-2^6 - 3^6)$ _____ j) $3^3 \times 4^0$ _____k) $(a+b)^0$ _____ l) $a^0 - b^0$ _____m) $-a^0 - b^0$ _____ n) $-(a+b)^0$ _____

10. Write as a repeated factor.

a) 2^4 _____ b) $(-2)^4$ _____c) -2^4 _____ d) a^4 _____e) $(-a)^5$ _____ f) a^5 _____

11. Use $<$, $>$ or $=$ to write a true sentence.

a) $2^3 \underline{<} 3^2$

b) $2^4 \underline{<} 4^2$

c) $(-2)^4 \underline{=} -2^4$

d) $-(-2)^3 \underline{<} 2^3$

e) $(-2)^6 \underline{>} 6^2$

f) $(-5)^3 \underline{<} (-3)^3$

g) $(-5)^0 \underline{>} (-4)^{\text{odd}}$

h) $(-2)^5 \underline{<} 5^2$

P.26 i) $\left(\frac{2}{3}\right)^2 \underline{>} \left(\frac{2}{3}\right)^5$ base is less than 1
smallest

j) $\left(\frac{5}{2}\right)^3 \underline{<} \left(\frac{5}{2}\right)^4$

m) $(-\frac{2}{3})^3 \underline{<} (-\frac{2}{3})^5$
 $-(\frac{2}{3})^3 < -(\frac{2}{3})^5 \Rightarrow (\frac{2}{3})^3 > (\frac{2}{3})^5$ smaller

n) $(-\frac{3}{2})^0 \underline{>} (-\frac{3}{2})^3$

o) $(-\frac{2}{3})^2 \underline{<} (-\frac{2}{3})^4$

12. Write in exponential form.

a) $2 + 2 + 2 + 2 = 8 = 2^3$

2^3

c) $5 + 5 + 5 + 5 + 5 =$

5^5

e) $6 + 6 + 6 + 6 + 6 + 6 = 36 \rightarrow 6^2$

g) $8 + 8 =$

8^2

13. Suppose the width of a square is four times the width of another square. How do the areas of the squares compare?

14. Suppose the volume of a cube is 343 times the volume of another cube. How do the lengths of the sides compare?

$$\begin{aligned} V &= l \times l \times l = 1 \\ V &= a \times a \times a \\ 343 &= a^3 \quad 343 = 7 \times 7 \times 7 \\ \therefore a &= 7 \text{ times bigger.} \end{aligned}$$

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Section 1.5 - Orders of Operations • 27

1.5

Orders of Operations

If we want to solve $4 + 2 \times 3$, do we add first, then multiply, or do we multiply first, then add? Does it make a difference? If we add first, the answer is 18; if we multiply first, the answer is 10. What if we write $2(3 + 4)$? What do the brackets mean? What about $6^2 \div 2$? To come to an answer that everyone can agree on, we must make rules to standardize the order in which we perform mathematical operations.

BEDMAS

Rules for Order of Operations

() [] { }

B. Do all calculations within brackets or parentheses first. When more than one kind of grouping symbol occurs, do the innermost one first, then work from the inside out.

E. Evaluate all exponential expressions.

D/M. Do all multiplication and division in order from left to right.

A/S. Do all addition and subtraction in order from left to right.

To remember the order of operations, the acronym BEDMAS is used.

B Brackets

E Exponents

D Division

M Multiplication

A Addition

S Subtraction

Ex2) $3 + 10 \cdot (4 + 2)^2$
1 Item

$$\begin{aligned} &= 3 + 10 \cdot 6^2 \\ &= 3 + 10 \cdot 36 \\ &= 3 + 360 \\ &= 363 \end{aligned}$$

Example 1 Simplify.

a) $5 + 3 \times 4$

$= 5 + 12$

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Example 1 Simplify.

a) $5 + 3 \times 4$
 $= 5 + 10 \times 36$
 $= 5 + 360$
 $= \boxed{365}$

b) $2^3 + 2 \times 3$
 $= (-3 \times 2)^2 - (4 + \frac{q^2}{3})$
 $\text{Ex3)} \quad (-6)^2 - \frac{4+27}{3} = \frac{q^2}{3} = \frac{q \cdot q}{3} = \frac{27}{3} = 27$

c) $6 - (2 + 3)^2$
 $= 6 - (3 + 2)^2$
 $= 6 - 36$
 $= \boxed{30}$

d) $(3 - 2 \times 4)^3 - (3 + \frac{6^2}{2})$
 $= (3 - 8)^3 - (3 + 36)$
 $= (-5)^3 - (3 + 18)$
 $= -125 - 21$
 $= \boxed{5}$

► Solution: a) $5 + 3 \times 4 = 5 + 12 = 17$
b) $2^3 + 2 \times 3 = 8 + 2 \times 3 = 8 + 6 = 14$
c) $6 - (2 + 3)^2 = 6 - 5^2 = 6 - 25 = -19$
d) $(3 - 2 \times 4)^3 - (3 + \frac{6^2}{2}) = (3 - 8)^3 - (3 + 36) = (-5)^3 - (3 + 18) = 25 - 21 = 4$

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28 • Chapter 1 - Square Roots, Powers, and Exponent Laws

1.5 Exercise Set P.28 HW p.28 Q 1-4 (R,lt)

1. Calculate.

a) $6 + 2 \times 3$ _____ b) $2 \times 3 + 2 \times 4$ _____

c) $4 \times 6 - 5 \times 3$ _____

d) $16 - 8 \div 4 - 2$ _____

P.28
e) $12 + 3 - 16 \div 8$
 $4 - 2$

2 _____ f) $25 - 18 + 6 - 10$ _____

g) $7 - 3 - 10 \div 2$ _____

h) $-6 \times 2 - 4 - 2$ _____

i) $6 - 3 \times 4 - 5$ _____

-11 _____ j) $63 \div 7 + 3 \times 2$ _____

2. Simplify.

a) $6 - (2 \times 3)$ _____

b) $(6 - 2) + 3$ _____

c) $-8 - (5 - 3)$ _____

d) $(-8 - 5) - 3$ _____

e) $-(8 - 3) + (3 - 7)$ _____

f) $100 \div (10 \div 5)$ _____

12. Write in exponential form.

g) $(100 \div 10) \div 5$ _____

h) $128 \div (32 \div 2)$ _____

i) $(128 \div 32) \div \frac{1}{2}$
 $\frac{128}{32} \times \frac{1}{2}$
 $\times \frac{1}{2}$

2 _____ j) $5 \times 10 - (7 + 3) \div 5 - 24$ _____

3. Simplify.

a) 3×2^3 _____

b) $(3 \times 2)^3$ _____

c) $-5 - 3^2$ _____

d) $(-5 - 3)^2$ _____

e) $2^4 + 2^2 \times 2^3 \div 2^3$ _____

f) $(2^4 \div 2^2)(2^3 \div 2^3)$ _____

g) $\frac{6 + 3 \times 4}{6 + 3 \times 4}$ _____

h) $\frac{(6 + 3)(4)}{6 + 3 \times 4}$ _____

i) $\frac{15 + 2 \times 5}{15 - 2 \times 5}$ _____

30) $\frac{(15 + 2)(5)}{15 - 2 \times 5}$ _____

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4. Simplify.

a) $12 \div 2[(20 - 8) - (1 + 3^2)]$

b) $\frac{3^2(1^3 + 2^3)}{2}$

Multiplying with Exponents

c) $4 + 3(2^2 - 1)^3$

d) $4^2[(8 + 4) \div 6]$

P.29

4 e) $\frac{(-5)^2 - 3 \times 5}{3^2 + 3 \times 2(-1)^3} = \frac{25 - 15}{9 + -6} = \boxed{\frac{10}{3}}$

f) $\frac{(-2)^3 + 4^3}{3 - 5^2 + 3 \times 6} = \frac{-8 + 64}{3 - 25 + 18} = \frac{56}{-4} = \boxed{-14}$

Ext

g) $4^2 \times 3 \div 8 = \frac{(4)(6 - 10)}{2} = \boxed{24 \div 2^3}$

h) $-5^2 + \frac{(3)(4 - 8)}{2} + 10 \div 5 =$

$= \frac{16 \times 3}{81} - \frac{2 \times (-4)}{21} = \frac{24}{8}$

$= 6 - 8 = \boxed{3}$

i) $2^3 \div 4 \times 2 + 3(5 - 2) - 3 \times 2 =$

j) $\frac{(6 - 5)^4 + 21}{27 - 4^2}$

$= \frac{8}{4} \times 2 + 9 - 6$

$= 4 + 9 - 6$

$= \boxed{7}$

k) $\frac{40 - 1^3 - 2^3}{3(2 + 5) + 2}$

P.29 TRY

m) $3 + 2\{3[(4 - 2)^2 + 1]\}$

n) $-6 - 3^2\{-2(2 - 3)^3 + (4 - 2)^2\}$

=

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$\rightarrow \boxed{-60}$

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