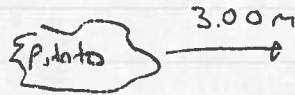



# Worksheet - 4.1 Work

① Work = Force  $\times$  distance

$$W = 20.0\text{ N} \cdot 1.5\text{ m} = 30.0\text{ N}\cdot\text{m} = 30\text{ J}$$

②  $W = F \cdot d = 6.00\text{ N} \cdot 3.00\text{ m} =$   
 $= \boxed{18.0\text{ J}}$

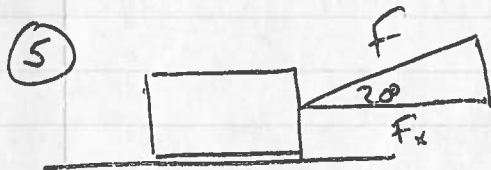


③  no distance = no work =  $\boxed{0\text{ J}}$

④ Find distance  $a = \frac{v^2}{2t} = \frac{11.0\text{ m/s}^2}{55} = 2.2\text{ m/s}^2$

$$d = \frac{v^2}{2a} = \frac{(11.0)^2}{2(2.2)} = 27.5\text{ m}$$

$$W = F \cdot d = m \cdot a \cdot d = (10.0\text{ kg}) \cdot (2.2\text{ m/s}^2) \cdot (27.5\text{ m}) = \boxed{605\text{ J}}$$



$$F_x = 75\text{ N} \cdot \cos(20^\circ) = 70.5\text{ N}$$

$$W = F_x \cdot d = 70.5\text{ N} \cdot 10.0\text{ m} = \boxed{705\text{ J}}$$

⑥  $W = F \cdot d = m \cdot g \cdot d = (60.0\text{ kg}) \cdot (9.8\text{ m/s}^2) \cdot (3.2\text{ m})$   
 $= \boxed{1900\text{ J}}$

⑦ No F  $W = F \cdot d = (0\text{ N}) \cdot (90\text{ m}) = \boxed{0\text{ J}}$

⑧  $W = F \cdot d = m \cdot g \cdot d_y = (80.0\text{ kg}) \cdot (9.8\text{ m/s}^2) \cdot (7.0\text{ m})$   
 $= \boxed{5500\text{ J}}$

⑨ Find  $F_{\text{app}}$

$$F_{\text{net}} = F_{\text{app}} - F_f$$

$$F_{\text{net}} + F_f = F_{\text{app}} = m \cdot a + F_f = (25.0\text{ kg}) \cdot 0.75\text{ m/s}^2 + 3.8\text{ N}$$

$$= 22.55\text{ N}$$

$$W = F \cdot d = 22.55\text{ N} \cdot 6.0\text{ m} = \boxed{140\text{ J}}$$

$$a = \frac{2d}{t^2} = \frac{2 \cdot (6.0)}{(4.0)^2} = 0.75\text{ m/s}^2$$

$$55 \text{ km/hr} = 15.27 \text{ m/s}$$

⑩ Find acceleration

$$v^2 = v_0^2 + 2ad$$

↖ Slowing down

$$\frac{v^2}{2d} = a = \frac{(15.27 \text{ m/s})^2}{2(38 \text{ m})} = -3.07 \text{ m/s}^2$$

$$W = F \cdot d = m \cdot a \cdot d = (1165 \text{ kg}) \cdot (-3.07 \text{ m/s}^2) \cdot (38 \text{ m}) = -1.4 \times 10^5 \text{ J}$$

### Worksheet 4.1 $E_p$ and $E_k$

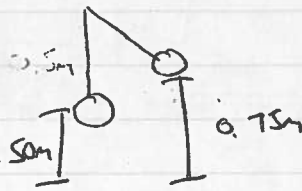
①  $E_p = m \cdot g \cdot h = 25.0 \text{ N} \cdot 2.10 \text{ m} = 52.5 \text{ J}$

②  $\Delta x = 20.0 \text{ cm} - 13.5 \text{ cm} = 6.5 \text{ cm} = 0.065 \text{ m}$

$$W = F \cdot \Delta x = (65 \text{ N}) (0.065 \text{ m}) = 4.225 \text{ J} = 4.2 \text{ J}$$

③  $E_p = m \cdot g \cdot h = (2.75 \text{ kg}) (9.8 \text{ m/s}^2) (7.00 \text{ m}) = 189 \text{ J}$

④  $\Delta h = 0.75 \text{ m} - 0.50 \text{ m} = 0.25 \text{ m}$

$$E_p = m \cdot g \cdot \Delta h = 2.0 \text{ kg} \cdot 9.8 \text{ m/s}^2 \cdot 0.25 \text{ m} = 4.9 \text{ J}$$


⑤  $E_p = m \cdot g \cdot h = (2.00 \times 10^3 \text{ kg}) (9.8 \text{ m/s}^2) (6.0 \text{ m}) = 1.2 \times 10^5 \text{ J}$

⑥  $E_k = \frac{1}{2} m v^2 = \frac{1}{2} (7.5 \text{ m/s})^2 (3.0 \text{ kg}) = 84 \text{ J}$

⑦  $E_k = \frac{1}{2} m v^2$   
 $v = \sqrt{\frac{2 E_k}{m}} = \sqrt{\frac{2 \cdot 500 \times 10^2 \text{ J}}{(200 \text{ N} / 9.8 \text{ m/s}^2)}} = 22.1 \text{ m/s}$

$$\textcircled{8} E_k = F_{\text{net}} \cdot d = m \cdot a \cdot d = \frac{F_g}{g} \cdot a \cdot d = \left( \frac{10.0 \text{ N}}{9.8 \text{ m/s}^2} \right) (2.5 \text{ m/s}^2) (15 \text{ m})$$

$$= \boxed{38 \text{ J}}$$

$$\textcircled{9} d = \cancel{\frac{1}{2} v_0 t} + \frac{1}{2} a t^2$$

$$d = \frac{1}{2} (9.8 \text{ m/s}^2) (4.5 \text{ s})^2 = 99.2 \text{ m}$$

$$E_k = F_{\text{net}} \cdot d = (1200.0 \text{ N}) \cdot (99.2 \text{ m}) = 1.2 \times 10^5 \text{ J}$$

$$\textcircled{10} E_k = E_p = m g h = (8.0 \text{ kg}) (9.8 \text{ m/s}^2) (7.0 \text{ m})$$

$$= 550 \text{ J}$$

$$\textcircled{11} E_p = E_k = (9.00 \text{ kg}) (1.2 \text{ m}) (9.8 \text{ m/s}^2) = 105.84 \text{ J}$$

$$E_k = \frac{1}{2} m v^2$$

$$v = \sqrt{\frac{2 E_k}{m}} = \sqrt{\frac{2 \cdot 105.84 \text{ J}}{9.00 \text{ kg}}} = \boxed{4.85 \text{ m/s}}$$

$$\textcircled{12} v_0 = 0$$

$$a = 9.8 \text{ m/s}^2$$

$$d = 7.2 \text{ m}$$

$$v_f = v$$

$$v_f = \sqrt{v_0^2 + 2ad}$$

$$= \sqrt{2(7.2)(9.8)} = 4.85 \text{ m/s}$$

### Worksheet - 4.1 Law of conservation of Energy

①

$$E_{pi} = E_{kf}$$

$$m g h = \frac{1}{2} m v^2$$

$$h = \frac{\frac{1}{2} v^2}{g} = \frac{(0.5) (3.2 \text{ m/s})^2}{9.8 \text{ m/s}^2} = 0.52 \text{ m}$$

$$\textcircled{2} \quad E_{pi} = E_{kf}$$

$$mgh = \frac{1}{2}mv^2$$

$$\sqrt{2gh} = v = \sqrt{2 \cdot (9.8) \cdot (8.0)} = \boxed{13 \text{ m}}$$

$$\textcircled{3} \quad E_p = E_{kf}$$

$$mgh = \frac{1}{2}mv^2$$

$$h = \frac{0.5v^2}{g} = \frac{(0.5) \cdot (37.0 \text{ m/s})^2}{(9.8 \text{ m/s}^2)} = \boxed{69.8 \text{ m}}$$

$$\textcircled{4} \quad E_{pi} + E_{ki} = E_{pf} + E_{kf}$$

$$mgh + \frac{1}{2}mv_i^2 = \frac{1}{2}mv_f^2$$

$$v_f = \sqrt{2gh + v_i^2}$$

$$= \sqrt{2(9.8 \text{ m/s}^2)(1.3 \times 10^2 \text{ m}) + (11.0 \text{ m/s})^2}$$

$$= \boxed{52 \text{ m/s}}$$

$$\textcircled{5} \quad E_{pi} + E_{ki} = E_{pf} + E_{kf}$$

see  
next  
page for 6!

$$mgh = \frac{1}{2}mv_f^2$$

$$v = \sqrt{2 \cdot g \cdot h} = \sqrt{2 \cdot (9.8 \text{ m/s}^2) \cdot (4.0 \text{ m})}$$

$$= \boxed{8.9 \text{ m/s}}$$

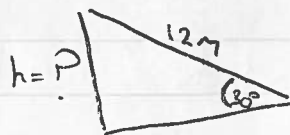
$$\textcircled{7} \quad E_{pi} + E_{ki} = E_{pf} + E_{kf}$$

$$mgh = \frac{1}{2}mv_f^2$$

$$v = \sqrt{2 \cdot g \cdot h}$$

$$= \sqrt{2 \cdot (9.8 \text{ m/s}^2) \cdot (6.00 \text{ m})}$$

$$= \boxed{10.8 \text{ m/s}}$$



$$h = 12 \cdot \sin(30^\circ) = 6.00 \text{ m}$$

⑥ all potential energy has been converted to kinetic energy

$$E_{p_i} + E_{k_i} = E_{p_f} + E_{k_f}$$

$$m \cdot g \cdot h = \frac{1}{2} m v_f^2$$
$$v_f = \sqrt{2 \cdot g \cdot h} = \sqrt{2 \cdot (9.8) \cdot (0.25)} = \boxed{2.2 \text{ m/s}}$$

⑧ A → C  $\Delta h = 8.0 \text{ m}$

$$E_{p_i} + E_{k_i} = E_{p_f} + E_{k_f}$$

$$m \cdot g \cdot h_a = m \cdot g \cdot h_c + \frac{1}{2} m v_f^2$$

$$v = \sqrt{2 \cdot g \cdot \Delta h}$$

$$v = \sqrt{2 \cdot (9.8 \text{ m/s}^2) \cdot (8.0 \text{ m})} = 13 \text{ m/s}$$

⑨

$$E_{p_i} = E_{k_f}$$

$$m \cdot g \cdot h = \frac{1}{2} m v_f^2$$

$$v = \sqrt{2 \cdot g \cdot h} = \sqrt{2 \cdot (9.8) \cdot (100)} = 14 \text{ m/s}$$

⑩

$$E_{p_i} + E_{k_i} = E_{p_f} + E_{k_f}$$

$$\frac{1}{2} m v_i^2 = m \cdot g \cdot h$$

$$h = \frac{0.5 v_i^2}{g} = \frac{0.5 \cdot (3.5)^2}{9.8 \text{ (m/s}^2)} = 0.625 \text{ m}$$
$$= \boxed{0.63 \text{ m}}$$

⑪

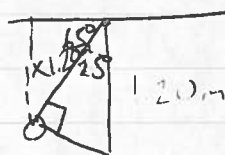
$$E_{p_i} + E_{k_i} = E_{p_f} + E_{k_f}$$

$$m \cdot g \cdot h = \frac{1}{2} m v_f^2$$

$$v = \sqrt{2 \cdot g \cdot h}$$

$$= \sqrt{2 \cdot 9.8 \cdot 0.1}$$

$$= \boxed{1.5 \text{ m/s}}$$



$$\sin(85^\circ) = \frac{h \cdot \sin}{1.20 \text{ m}} ; x = 1.09 \text{ m}$$

$$h = 1.20 \text{ m} - 1.09 \text{ m} = 0.11 \text{ m}$$

## Worksheet 4.2 - Power and Efficiency

①  $P = \frac{W}{\Delta t}$

$$\Delta t = \frac{W}{P} = \frac{m \cdot g \cdot d}{P} = \frac{45.0 \text{ kg} \cdot 9.8 \text{ m/s}^2 \cdot 6.0 \text{ m}}{1.50 \times 10^3 \text{ W}} = \boxed{1.8 \text{ s}}$$

②  $P = \frac{W}{\Delta t} = \frac{F_g \cdot d}{\Delta t} = \frac{20.0 \text{ kg} \cdot 9.8 \text{ m/s}^2 \cdot 2.50 \text{ m}}{2.05} = \boxed{245 \text{ W}}$

③  $P = \frac{W}{\Delta t} = \frac{\Delta E}{\Delta t} = \frac{\frac{1}{2} m v^2}{\Delta t} = \frac{\frac{1}{2} \cdot 2.00 \text{ kg} \cdot (3.00 \text{ m/s})^2}{1.5 \text{ m}} = 9.0 \text{ W}$

$$d = \left( \frac{v_f^2 + v_i^2}{2} \right) t$$

$$t = \frac{2d}{v_f} = \frac{2(1.5 \text{ m})}{(3.0 \text{ m/s})} = 1.0 \text{ s}$$

④  $P_{\text{out}} = \frac{W}{\Delta t} = F \left( \frac{d}{t} \right) = F \cdot v = m g v = (8.50 \times 10^2 \text{ kg}) (9.8 \text{ m/s}^2) (1.00 \text{ s}) = \boxed{8.3 \times 10^3 \text{ W}}$

⑤  $P_{\text{in}} = 10,000 \text{ W}$       $\text{Eff} = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{8.3 \times 10^3 \text{ W}}{10 \times 10^4 \text{ W}} \times 100\% = 83\%$

⑥  $P = \frac{W}{\Delta t} = \frac{F_{\text{app}} \cdot d}{\Delta t} = \frac{(49 \text{ N}) (2.0 \text{ m})}{0.67 \text{ sec}} = \boxed{1.5 \times 10^2 \text{ W}}$

$$v_f^2 = v_i^2 + 2ad$$

$$a = \frac{v_f^2}{2d} = \frac{(6.0)^2}{2 \cdot (2)} = 9.0 \text{ m/s}^2$$

$$d = \left( \frac{v_i + v_f}{2} \right) t$$

$$\frac{2d}{v_f} = t = \frac{2 \cdot (2)}{6} = 0.67 \text{ sec}$$

$$F_{\text{net}} = F_{\text{app}} - F_f$$

$$F_{\text{app}} = (9.0 \text{ m/s}^2) (5.0 \text{ kg}) + 4.0 \text{ N} = \boxed{49 \text{ N}}$$

⑥

$$P_{in} = 5.00 \times 10^2 \text{ W}$$

$$P_{out} = \frac{W}{\Delta t} = \frac{m \cdot g \cdot h}{\Delta t} = \frac{20.0 \text{ kg} \cdot 9.8 \text{ m/s}^2 \cdot 5.00 \text{ m}}{3.50 \text{ s}}$$

$$= 280 \text{ W}$$

$$\text{Eff} = \frac{P_{out}}{P_{in}} \times 100\% = \frac{280 \text{ W}}{5.00 \times 10^2 \text{ W}} = 56\%$$

⑦

$$\text{Eff} = \frac{P_{out}}{P_{in}} \times 100\% = 82\%$$

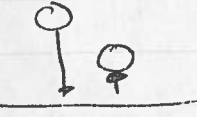
$$P_{out} = \frac{82}{100} \times 1.00 \times 10^3 \text{ W} = 820 \text{ W}$$

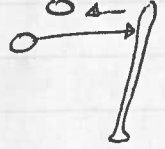
$$P = \frac{\Delta W}{\Delta t}$$

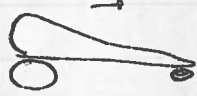
$$\Delta t = \frac{W}{P} = \frac{m \cdot g \cdot d}{P} = \frac{(50.0 \text{ kg})(9.8 \text{ m/s}^2)(15.0 \text{ m})}{820 \text{ W}}$$

$$= 0.896 \text{ sec}$$

### 43 - Momentum

①   $\Delta p = m \cdot \Delta v = 1.0 \text{ kg} (1.0 \text{ m/s} - (-2.0 \text{ m/s})) = \boxed{3.0 \text{ kg} \cdot \text{m/s}}$   
 $u_p = +$

②   $\Delta p = m \Delta v = 0.144 \text{ kg} (-38 \text{ m/s} - 38 \text{ m/s}) = \boxed{-10.9 \text{ kg} \cdot \text{m/s}}$

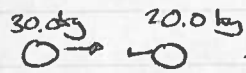
③   $a = 12.5 \text{ m/s}^2$   
 $t = 3.25 \text{ s}$   
 $v_f = v_i + at = 10 \text{ m/s} + (12.5 \text{ m/s}^2 \cdot 3.25 \text{ s}) = \boxed{50.625 \text{ m/s}}$

$v_i = 36 \text{ km/hr} = 10 \text{ m/s}$

$v_f = 50.625 \text{ m/s}$

$m = 800 \text{ kg}$

$\Delta p = m \cdot \Delta v = 800 \text{ kg} \cdot (50.625 \text{ m/s} - 10 \text{ m/s}) = \boxed{32,500 \text{ kg} \cdot \text{m/s}}$

  $30.0 \text{ kg} \quad 20.0 \text{ kg}$

④  $m_{1i} v_{1i} + m_{2i} v_{2i} = m_{1f} v_{1f} + m_{2f} v_{2f}$   
 $(30.0)(1.00) + (20.0)(-5.00) = (30.0) v_{1f} + (20.0)(-1.25)$

$v_{1f} = -1.5 \text{ m/s}$  or  $\boxed{1.5 \text{ m/s left}}$

⑤   $\rightarrow$  inelastic

$m_1 v_1 + m_2 v_2 = m_+ v_+$

$(4.50 \times 10^3 \text{ kg})(5.00 \text{ m/s}) = (4.50 \times 10^3 \text{ kg} + 6.50 \times 10^3 \text{ kg}) v_+$

$v_+ = \boxed{2.05 \text{ m/s east}}$

⑥  inelastic

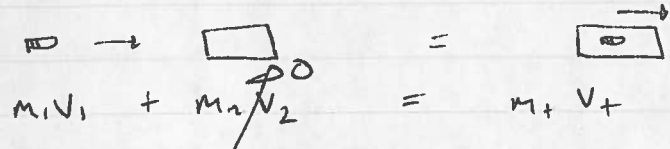
$m_1 v_1 + m_2 v_2 = m_+ v_+$

$925 \text{ kg} \cdot 18.0 \text{ m/s} = (925 + m_2) 6.50 \text{ m/s}$

$\frac{925 \text{ kg} \cdot 18.0 \text{ m/s} - 925 \text{ kg} \cdot 6.50 \text{ m/s}}{6.50 \text{ m/s}} = m_2$

$m_2 = \boxed{1640 \text{ kg}}$



7  inelastic

$$m_1 v_1 + m_2 v_2 = m_+ v_+$$

$$0.050 \text{ kg} \cdot v_1 = (0.050 \text{ kg} + 7.00 \text{ kg}) 5.00 \text{ m/s}$$

$$v_1 = 705 \text{ m/s}$$

8  inelastic

$$m_1 v_1 + m_2 v_2 = m_+ v_+$$

$$(0.040 \text{ kg})(9.00 \text{ m/s}) + (0.055 \text{ kg})(6.00 \text{ m/s}) = (0.040 \text{ kg} + 0.055 \text{ kg}) v_+$$

$$v_+ = 0.316 \text{ m/s}$$

9  $\Delta p = 0$

student                  cream pie

↓                                  ↓

$$m_+ v_+ = m_1 v_1 + m_2 v_2$$

$$0 = (16 \text{ kg}) v_1 + (0.20 \text{ kg})(22 \text{ m/s})$$

$$v_1 = 0.058 \text{ m/s right}$$

10

turkey                  turkey launcher

↓                                  ↓

$$m_+ v_+ = m_1 v_1 + m_2 v_2$$

$$0 = (255 \text{ kg})(325 \text{ m/s}) + (1.1 \times 10^3 \text{ kg}) v_2$$

$$v_2 = -7.386 \text{ m/s}$$

$$v_2 = 7.4 \text{ m/s West}$$

11

gases                  vehicle

↓                                  ↓

$$m_+ v_+ = m_1 v_1 + m_2 v_2$$

$$0 = (4.5 \times 10^2 \text{ kg})(1.4 \times 10^3 \text{ m/s}) + (m_2)(-45 \text{ m/s})$$

$$m_2 = 1.4 \times 10^4 \text{ kg}$$

### 4.3 - Impulse

①  $\Delta p = m \Delta v = F_{\text{net}} \cdot t$

$$\Delta v = \frac{F_{\text{net}} \cdot t}{m} = \frac{(1.5 \times 10^5 \text{ N})(15 \text{ s})}{(9.5 \times 10^3 \text{ kg})} = \boxed{237 \text{ m/s}}$$

②  $m \cdot \Delta v = F_{\text{net}} \cdot t$

$$F_{\text{net}} = \frac{m \cdot \Delta v}{t} = \frac{263 \text{ kg} (-21.0 \text{ m/s})}{2.60 \text{ s}} = -212 \text{ N} = \boxed{212 \text{ N south}}$$

③  $\Delta p = m \Delta v = 15.0 \text{ kg} (10.0 \text{ m/s} - 0 \text{ m/s}) = \boxed{150 \text{ N} \cdot \text{s south}}$

④  $\Delta p = F_{\text{net}} \cdot t = (25.0 \text{ N}) \cdot (7.20 \times 10^{-1} \text{ s}) = \boxed{18 \text{ N} \cdot \text{s North}}$

⑤  $\Delta p = m \cdot \Delta v = 5.00 \text{ kg} \cdot (15.0 \text{ m/s} - 0 \text{ m/s}) = 75 \text{ N} \cdot \text{s East}$

⑥  $d = v_0 t + \frac{1}{2} a t^2$

$$a = \frac{2d}{t^2} = 5.14 \text{ m/s}^2$$

$$v = v_0 + at = 16.44 \text{ m/s}$$

$$\Delta p = m \cdot \Delta v = (11.0 \text{ kg})(-16.44 \text{ m/s} - 0 \text{ m/s}) = 181 \text{ kg m/s} = \boxed{181 \text{ N} \cdot \text{s west}}$$

⑦  $\Delta p = m \cdot \Delta v$

$$\Delta v = \frac{\Delta p}{m} = \frac{6.80 \text{ kg} \cdot \text{m/s}}{1.430 \text{ kg}} = 4.615 \text{ m/s} = v_f$$

$$a = 9.8 \text{ m/s}^2$$

$$v_f^2 = v_0^2 + 2ad$$

$$\frac{v_f^2}{2a} = \frac{(4.615 \text{ m/s})^2}{2(9.8 \text{ m/s}^2)} = \boxed{1.1 \text{ m down}}$$

$$\textcircled{8} \Delta p = m \Delta v = F_{\text{net}} \cdot t$$

$$m = \frac{F_{\text{net}} \cdot t}{\Delta v} = \frac{16.0 \text{ N} \cdot 2.00 \times 10^{-1} \text{ s}}{3.50 \text{ m/s}} = \boxed{0.91 \text{ kg}}$$

9 a)



$$F_{\text{net}} = F_{\text{app}} - F_{\text{W}}$$

$$= 8.20 \text{ N} - (0.500 \text{ kg})(9.8 \text{ m/s}^2)$$

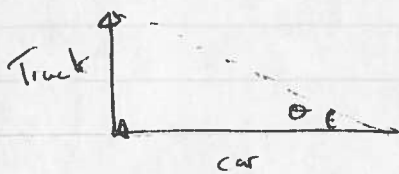
$$= 3.3 \text{ N}$$

$$\textcircled{b} a = \frac{F_{\text{net}}}{m} = 6.6 \text{ m/s}^2 \rightarrow t = \sqrt{\frac{2d}{a}} = 0.67425$$

$$\Delta v = \frac{F_{\text{net}} \cdot t}{m} = \frac{(3.3 \text{ N}) \cdot (0.67425 \text{ s})}{(0.500 \text{ kg})} = \boxed{4.45 \text{ m/s}}$$

## 4.4 - Collisions

①

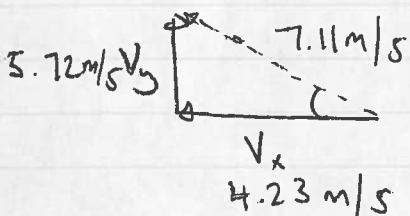


car =  $1.4 \times 10^3 \text{ kg}$   $37.0 \text{ km/hr} = 10.28 \text{ m/s}$   
 truck =  $2.0 \times 10^3 \text{ kg}$   $35 \text{ km/hr} = 9.72 \text{ m/s}$

Break down into components

$$m_1 v_{1x} + m_2 v_{2x} = m_{tx} v_{tx}$$

$$v_{tx} = \frac{(1.4 \times 10^3)(10.28)}{(3.4 \times 10^3)} = 4.23 \text{ m/s}$$

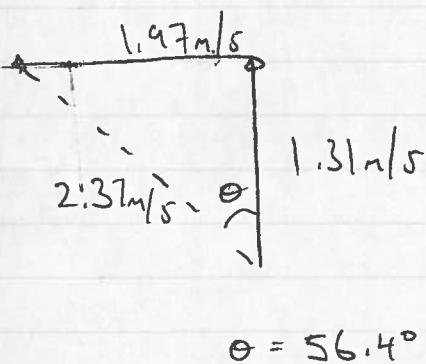


$$m_1 v_{1y} + m_2 v_{2y} = m_{ty} v_{ty}$$

$$v_{ty} = \frac{(2.0 \times 10^3)(9.72)}{3.4 \times 10^3} = 5.72 \text{ m/s}$$

**7.11 m/s  $37^\circ$  W of N**

②



$$m_1 v_{1x} + m_2 v_{2x} = m_{tx} v_{tx}$$

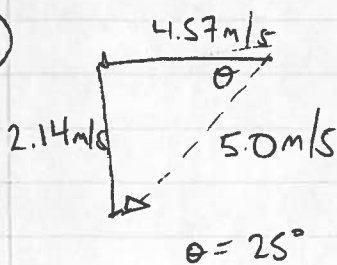
$$\frac{(8.0)(3.5)}{(14.2)} = v_{tx} = 1.97 \text{ m/s}$$

$$m_1 v_{1y} + m_2 v_{2y} = m_{ty} v_{ty}$$

$$\frac{(6.2)(3.0)}{(14.2)} = 1.31 \text{ m/s}$$

**2.37 m/s  $56.4^\circ$  W of N**

③



$$m_1 v_{1x} + m_2 v_{2x} = m_{tx} v_{tx}$$

$$v_{tx} = \frac{(4.08 \times 10^3)(8.0)}{(7.14 \times 10^3)} = 4.57 \text{ m/s}$$

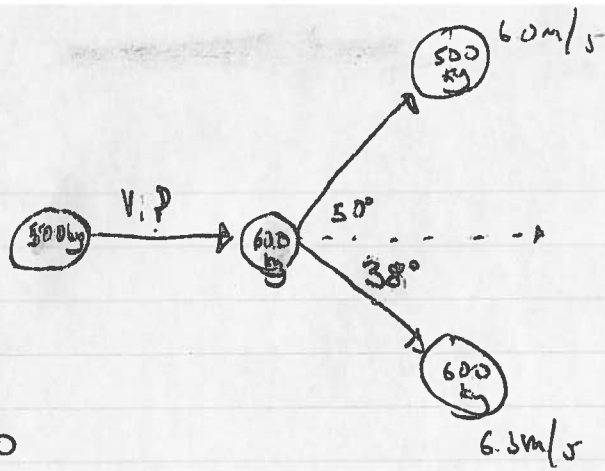
Truck<sub>1</sub> =  $4.08 \times 10^3 \text{ kg}$   
 Truck<sub>2</sub> =  $3.06 \times 10^3 \text{ kg}$

$$m_1 v_{1y} + m_2 v_{2y} = m_{ty} v_{ty}$$

$$v_{ty} = \frac{(3.06 \times 10^3)(5.0)}{(7.14 \times 10^3)} = 2.14$$

**5.0 m/s  $25^\circ$  S of W**

4



a)  $\Delta p_x = 0$   
 $\sum p_{xi} = \sum p_{xf}$

$$m_{50} v_{ix} = m_{50} v_{fx} + m_{60} v_{fx}$$

$$(500)(v_{ix}) = (500)(6.0) \cos(50^\circ) + (600)(6.3) \cos(38^\circ)$$

$$v_{ix} = v_i = 9.81 \text{ m/s}$$

b) does  $E_{ki} = E_{kf}$ ?

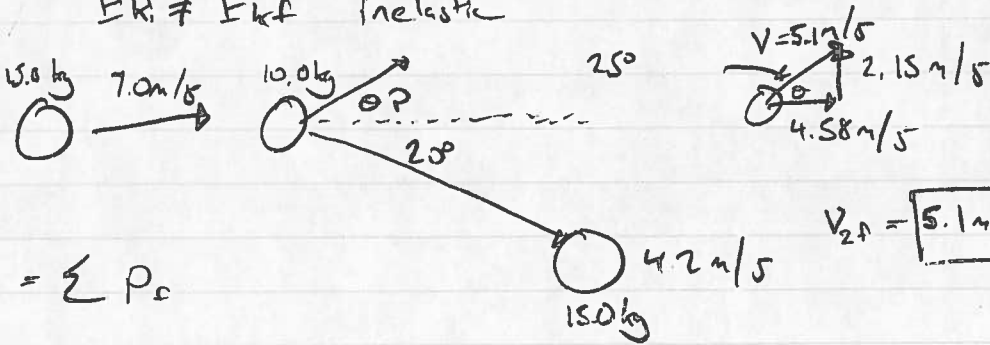
$$E_{ki} = \frac{1}{2} m v^2 = \frac{1}{2} (500)(9.81)^2 = 2.41 \times 10^3 \text{ J}$$

$$E_{kf} = \frac{1}{2} m v^2 = \frac{1}{2} (500)(6.0)^2 + \frac{1}{2} (600)(6.3)^2$$

$$= 2.09 \times 10^3 \text{ J}$$

$E_{ki} \neq E_{kf}$  inelastic

5



a)

$$\sum p_i = \sum p_f$$

$$\sum p_{ix} = \sum p_{fx}$$

$$m_{15} v_{ix} = m_{15} v_{fx} + m_{10} v_{fx}$$

$$(15.0)(7.0) = (15.0)(4.2) \cos(20^\circ) + 10 v_{fx}$$

$$\frac{(15.0)(7.0) - (15.0)(4.2) \cos(20^\circ)}{10} = v_{fx} = 4.58 \text{ m/s}$$

$$v_{2f} = \boxed{5.1 \text{ m/s } 25^\circ \text{ N of E}}$$

$$0 = m_{15f} v_{15yf} + m_{10f} v_{10yf}$$

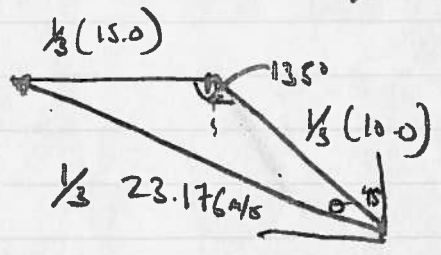
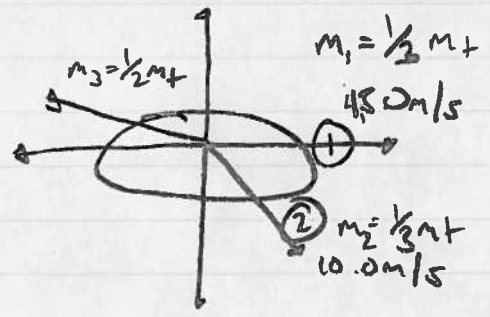
$$v_{2yf} = -\left(\frac{m_{15f} v_{15yf}}{m_{10f}}\right) = \frac{(15.0)(4.2) \cdot \sin(20^\circ)}{(10.0)} = 2.15 \text{ m/s}$$

∴ does  $E_{ki} = E_{kf}$  NO! inelastic

$$E_{ki} = \frac{1}{2} m v^2 = (0.5)(15.0)(7.0 \text{ m/s})^2 = 367.5 \text{ J}$$

$$E_{kf} = (0.5)(15.0)(4.2)^2 + (0.5)(10.0)(5.1)^2 = 262.4 \text{ J}$$

⑥



$$c^2 = a^2 + b^2 - 2ab \cos(C)$$

$$c = \sqrt{(15)^2 + (10)^2 - 2(15)(10) \cos(135)} = 23.176 \text{ m/s}$$

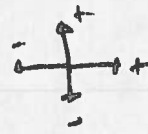
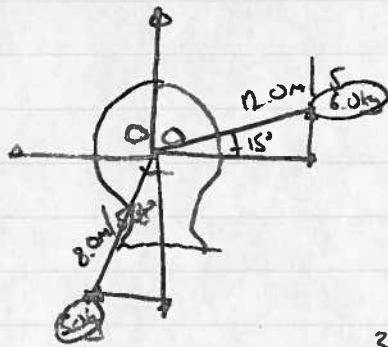
$$\frac{\sin(C)}{c} = \frac{\sin(A)}{a}$$

$$\frac{a \sin(C)}{c} = \sin A = \left( \frac{15.0}{23.176} \right) \cdot \sin(135) = 0.4576$$

$$A = \sin^{-1}(0.4576) = 27.24^\circ$$

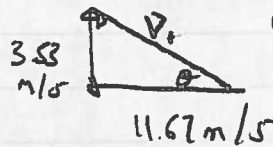
23.2 m/s 17.8° N of E

Special!



3rd piece = 4.0 kg

$$v_f = 12.2 \text{ m/s}$$
$$\theta = 16.8^\circ$$



$$\sum p_x = 0$$

$$\sum p_{xi} = \sum p_{xf}$$

$$0 = p_{1f} + p_{2f} + p_{3f} = (6.0)(12.0) \cdot \cos(15) + 5.0(8.0) \cdot \sin(35) + 4.0 v_{3x}$$

$$v_{3x} = \frac{22.9 \text{ N}\cdot\text{s} - 69.54 \text{ N}\cdot\text{s}}{4.0 \text{ kg}}$$
$$= -11.67 \text{ m/s}$$

$$\sum p_y = 0$$

$$\sum p_{yi} = \sum p_{yf}$$

$$0 = (6.0)(12.0) \cdot \sin(15) + (5.0)(8.0) \cdot \cos(35) + 4.0 v_{3y}$$

$$v_{3y} = \frac{32.77 \text{ N}\cdot\text{s} - 18.63 \text{ N}\cdot\text{s}}{4.0 \text{ kg}} = 3.53 \text{ m/s}$$

4.0 kg piece 12.2 m/s 17° N of W